SNAPSHOT

GEOMETRY

Snapshot – Geometry

Mathematical Process Standards

G.1   Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding.

Tools to Know

G.1(A)   apply mathematics to problems arising in everyday life, society, and the workplace

G.1(B)   use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution

G.1(C)   select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems

Coordinate and Transformational Geometry
Connected Knowledge and Skills G.12

G.2   Coordinate and transformational geometry. The student uses the process skills to understand the connections between algebra and geometry and uses the one- and two-dimensional coordinate systems to verify geometric conjectures.

G.3   Coordinate and transformational geometry. The student uses the process skills to generate and describe rigid transformations (translation, reflection, and rotation) and non-rigid transformations (dilations that preserve similarity and reductions and enlargements that do not preserve similarity).

Readiness Standards	Supporting Standards
G.2(B) derive and use the distance, slope, and midpoint formulas to verify geometric relationships, including congruence of segments and parallelism or perpendicularity of pairs of lines G.2(C) determine an equation of a line parallel or perpendicular to a given line that passes through a given point G.3(B) determine the image or pre-image of a given two-dimensional figure under a composition of rigid transformations, a composition of non-rigid transformations, and a composition of both, including dilations where the center can be any point in the plane	G.2(A) determine the coordinates of a point that is a given fractional distance less than one from one end of a line segment to the other in one- and two-dimensional coordinate systems, including finding the midpoint G.3(A) describe and perform transformations of figures in a plane using coordinate notation G.3(C) identify the sequence of transformations that will carry a given pre-image onto an image on and off the coordinate plane G.3(D) identify and distinguish between reflectional and rotational symmetry in a plane figure G.12(E) show that the equation of a circle with center at the origin and radius r is $x^2 + y^2 = r^2$ and determine the equation for the graph of a circle with radius r and center (h, k), $(x - h)^2 + (y - k)^2 = r^2$

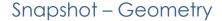## Logical Argument and Constructions
Connected Knowledge and Skills G.12

G.4   Logical argument and constructions. The student uses the process skills with deductive reasoning to understand geometric relationships.

G.5   Logical argument and constructions. The student uses constructions to validate conjectures about geometric figures.

G.6   Proof and congruence. The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.

G.4(C) verify that a conjecture is false using a counterexample G.5(A) investigate patterns to make conjectures about geometric relationships, including angles formed by parallel lines cut by a transversal, criteria required for triangle congruence, special segments of triangles, diagonals of quadrilaterals, interior and exterior angles of polygons, and special segments and angles of circles choosing from a variety of tools G.6(A) verify theorems about angles formed by the intersection of lines and line segments, including vertical angles, and angles formed by parallel lines cut by a transversal and prove equidistance between the endpoints of a segment and points on its perpendicular bisector and apply these relationships to solve problems	G.4(A) distinguish between undefined terms, definitions, postulates, conjectures, and theorems G.4(B) identify and determine the validity of the converse, inverse, and contrapositive of a conditional statement and recognize the connection between a biconditional statement and a true conditional statement with a true converse G.4(D) compare geometric relationships between Euclidean and spherical geometries, including parallel lines and the sum of the angles in a triangle G.5(B) construct congruent segments, congruent angles, a segment bisector, an angle bisector, perpendicular lines, the perpendicular bisector of a line segment, and a line parallel to a given line through a point not on a line using a compass and a straightedge G.5(C) use the constructions of congruent segments, congruent angles, angle bisectors, and perpendicular bisectors to make conjectures about geometric relationships G.5(D) verify the Triangle Inequality theorem using constructions and apply the theorem to solve problems G.6(E) prove a quadrilateral is a parallelogram, rectangle, square, or rhombus using opposite sides, opposite angles, or diagonals and apply these relationships to solve problems G.12(A) apply theorems about circles, including relationships among angles, radii, chords, tangents, and secants, to solve non-contextual problems

Triangles and Trigonometry
Connected Knowledge and Skills G.5

G.6 Proof and congruence. The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.

G.7 Similarity, proof, and trigonometry. The student uses the process skills in applying similarity to solve problems.

G.8 Similarity, proof, and trigonometry. The student uses the process skills with deductive reasoning to prove and apply theorems by using a variety of methods such as coordinate, transformational, and axiomatic and formats such as two-column, paragraph, and flow chart.

G.9 Similarity, proof, and trigonometry. The student uses the process skills to understand and apply relationships in right triangles.

Readiness Standards	Supporting Standards
G.5(A) investigate patterns to make conjectures about geometric relationships, including angles formed by parallel lines cut by a transversal, criteria required for triangle congruence, special segments of triangles, diagonals of quadrilaterals, interior and exterior angles of polygons, and special segments and angles of circles choosing from a variety of tools	G.6(C) apply the definition of congruence, in terms of rigid transformations, to identify congruent figures and their corresponding sides and angles
G.6(B) prove two triangles are congruent by applying the Side-Angle-Side, Angle-Side-Angle, Side-Side-Side, Angle-Angle-Side, and Hypotenuse-Leg congruence conditions	G.6(D) verify theorems about the relationships in triangles, including proof of the Pythagorean Theorem, the sum of interior angles, base angles of isosceles triangles, midsegments, and medians, and apply these relationships to solve problems
G.7(B) apply the Angle-Angle criterion to verify similar triangles and apply the proportionality of the corresponding sides to solve problems	G.7(A) apply the definition of similarity in terms of a dilation to identify similar figures and their proportional sides and the congruent corresponding angles
G.9(A) determine the lengths of sides and measures of angles in a right triangle by applying the trigonometric ratios sine, cosine, and tangent to solve problems	G.8(A) prove theorems about similar triangles, including the Triangle Proportionality theorem, and apply these theorems to solve problems
G.9(B) apply the relationships in special right triangles 30°-60°-90° and 45°-45°-90° and the Pythagorean theorem, including Pythagorean triples, to solve problems	G.8(B) identify and apply the relationships that exist when an altitude is drawn to the hypotenuse of a right triangle, including the geometric mean, to solve problems

Measurement of 2D and 3D Figures

G.10 Two-dimensional and three-dimensional figures. The student uses the process skills to recognize characteristics and dimensional changes of two- and three-dimensional figures.

G.11 Two-dimensional and three-dimensional figures. The student uses the process skills in the application of formulas to determine measures of two- and three-dimensional figures.

G.12 Circles. The student uses the process skills to understand geometric relationships and apply theorems and equations about circles.

G.10(B) determine and describe how changes in the linear dimensions of a shape affect its perimeter, area, surface area, or volume, including proportional and non-proportional dimensional change	G.10(A) identify the shapes of two-dimensional cross-sections of prisms, pyramids, cylinders, cones, and spheres and identify three-dimensional objects generated by rotations of two-dimensional shapes
G.11(B) determine the area of composite two-dimensional figures comprised of a combination of triangles, parallelograms, trapezoids, kites, regular polygons, or sectors of circles to solve problems using appropriate units of measure	G.11(A) apply the formula for the area of regular polygons to solve problems using appropriate units of measure
G.11(C) apply the formulas for the total and lateral surface area of three-dimensional figures, including prisms, pyramids, cones, cylinders, spheres, and composite figures, to solve problems using appropriate units of measure	G.12(B) apply the proportional relationship between the measure of an arc length of a circle and the circumference of the circle to solve problems
G.11(D) apply the formulas for the volume of three-dimensional figures, including prisms, pyramids, cones, cylinders, spheres, and composite figures, to solve problems using appropriate units of measure	G.12(C) apply the proportional relationship between the measure of the area of a sector of a circle and the area of the circle to solve problems
	G.12(D) describe radian measure of an angle as the ratio of the length of an arc intercepted by a central angle and the radius of the circle

Probability

G.13 Probability. The student uses the process skills to understand probability in real-world situations and how to apply independence and dependence of events.

G.13(C) identify whether two events are independent and compute the probability of the two events occurring together with or without replacement	G.13(A) develop strategies to use permutations and combinations to solve contextual problems
	G.13(B) determine probabilities based on area to solve contextual problems
	G.13(D) apply conditional probability in contextual problems
	G.13(E) apply independence in contextual problems

Mathematical Process Standards

G.1   Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding.

Ways to Show

G.1(D)   communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate
G.1(E)   create and use representations to organize, record, and communicate mathematical ideas
G.1(F)   analyze mathematical relationships to connect and communicate mathematical ideas
G.1(G)   display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication

NOTE: The classification of standards on this Snapshot represents the reviewed and synthesized input of a sample of Texas Math teachers. This Snapshot DOES NOT represent a publication of the Texas Education Agency. District curriculum may reflect other classifications.